

# Compilers and computer architecture: Just-in-time compilation

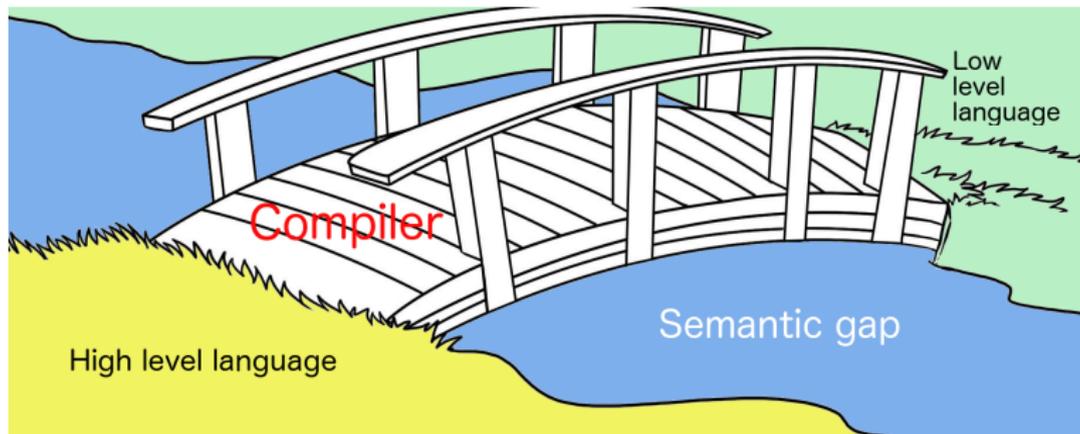
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December 2019

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Chi-2R312

# Recall the function of compilers



Welcome to the cutting edge

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Compilers are used to translate from programming languages humans can understand to machine code executable by computers. Compilers come in two forms:

- ▶ Conventional **ahead-of-time** compilers where translation is done once, long before program execution.
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We spend the whole term learning about the former. Today I want to give you a **brief** introduction to the latter.

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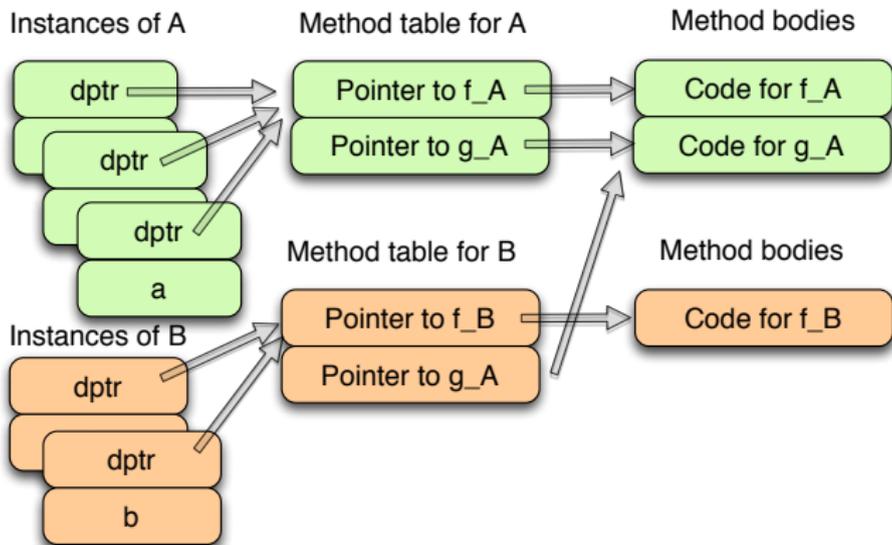
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JIT compilers are cutting (bleeding) edge technology and considerably more complex than normal compilers, which are already non-trivial. Hence the presentation today will be massively simplifying.

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Let's look at two examples. Remember the compilation of objects and classes?



To deal with inheritance of methods, invoking a method is indirect via the method table. Each invocation has to follow two pointers. Without inheritance, no need for indirection.

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Of course an individual indirection takes  $< 1$  nano-second on a modern CPU. So why worry? Answer: loops!

```
interface I {
    int f ( int n ); }

class A implements I {
    public int f ( int n ) { return n; } }

class B implements I {
    public int f ( int n ) { return 2*n; } }

class Main {
    public static void main ( String [] args ) {
        I o = new A ();
        for ( int i = 0; i < 1000000; i++ ) {
            for ( int j = 0; i < 1000000; j++ ) {
                o.f ( i+j ); } } } }
```

Performance penalties add up.

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Yes, in this simple example, a good optimising compiler can do this. But what about the following?

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```
public static void main ( String [] args ) {  
    I o = null;  
    if ( args [ 0 ] == "hello" )  
        new A ();  
    else  
        new B ();  
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(Aside, can you see a hack to deal with this problem in an AOT compiler?)

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Simplifying a little, variables in dynamically typed languages store not just the usual value, e.g. 3, but also the type of the value, e.g. `Int`, and sometimes even more. Whenever you carry an innocent operation like

```
x = x + y
```

under the hood something like the following happens.

```
let tx = typeof ( x )
let ty = typeof ( y )
if ( tx == Int && ty == Int )
    let vx = value ( x )
    let vy = value ( y )
    let res = integer_addition ( vx, vy )
    x_result_part = res
    x_type_part = Int
else
    ... // even more complicated.
```

# If JIT compilers are the answer ... what is the problem?

Imagine this in a nested loop!

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for ( int i = 0; i < 1000000; i++ ) {  
    for ( int j = 0; i < 1000000; j++ ) {  
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        ...  
    }  
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```

This is painful. This is why dynamically typed languages are slow(er).

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Because typically innermost loops work on big and uniform data structures (usually big arrays).

So the compiler should move the type-checks outside the loops.

# If JIT compilers are the answer ... what is the problem?

Recall that in dynamically typed languages

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for ( int i = 0; i < 1000000; i++ ) {  
  for ( int j = 0; i < 1000000; j++ ) {  
    a [i, j] = a[i, j] + 1 } }
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Is really

```
for ( int i = 0; i < 1000000; i++ ) {  
  for ( int j = 0; i < 1000000; j++ ) {  
    let ta = typeof ( a[i, j] ) // always same  
    let t1 = typeof ( 1 )      // always same  
    if ( ta == Int && t1 == Int ) {  
      let va = value ( a[i, j] )  
      let v1 = value ( 1 ) // simplifying  
      let res = integer_addition ( va, v1 )  
      a[ i, j ]_result_part = res  
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## If JIT compilers are the answer ... what is the problem?

So program from last slide can be

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let ta = typeof ( a )
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Alas, at compile-time, the compiler does not have enough information to make this optimisation safely.

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Let's summarise the situation.

- ▶ Certain powerful optimisations cannot be done at compile-time, because the compiler has not got enough information to know they are safe.
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Hmmm, what could we do ...





How about we compile and optimise only at run-time?



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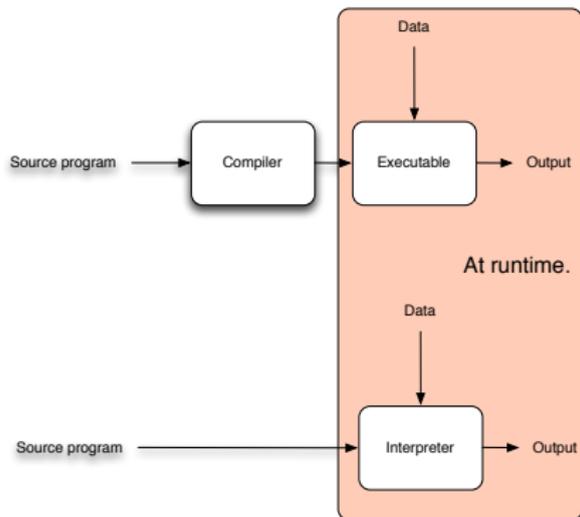
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Enter **interpreters!**

# Interpreters

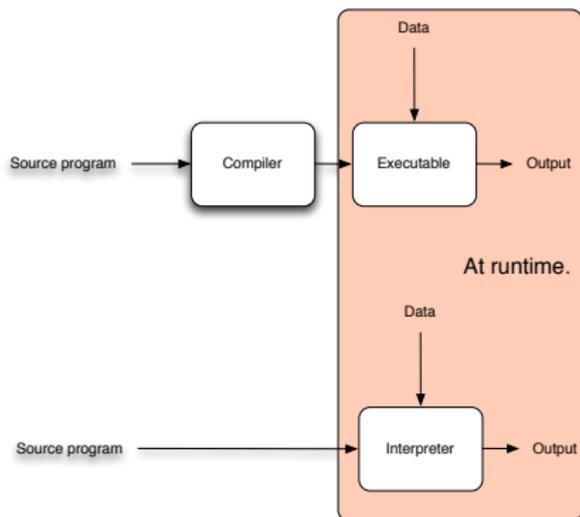
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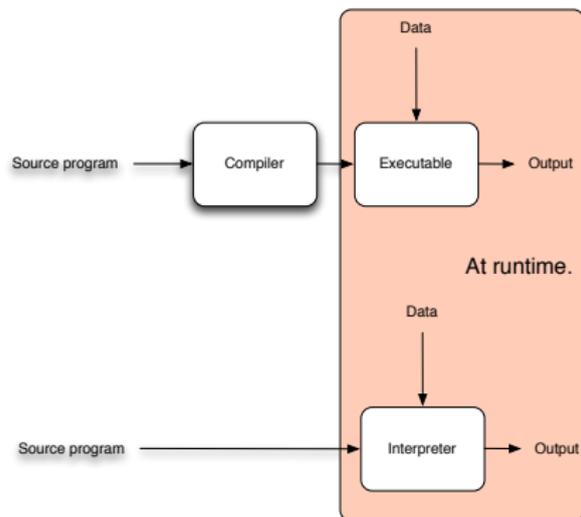
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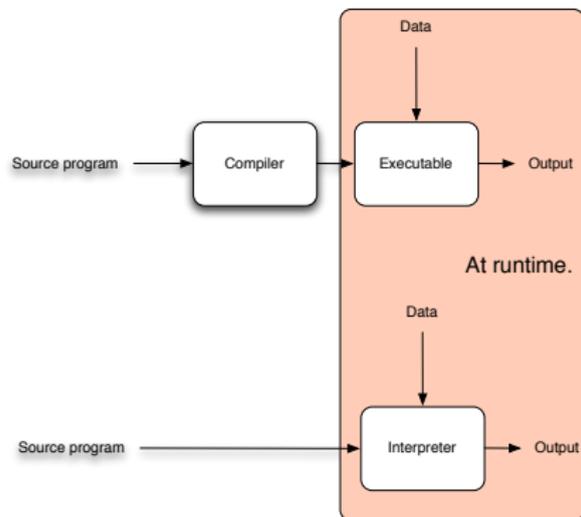
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- ▶ Compilers generate a program that has an effect on the world.
- ▶ Interpreters effect the world directly.

# Interpreters

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- ▶ The advantage of compilers is that generated code is **faster**, because a lot of work has to be done only once (e.g. lexing, parsing, type-checking, optimisation). And the results of this work are shared in every execution. The interpreter has to redo this work every time.
- ▶ The advantage of interpreters is that they are much **simpler** than compilers.

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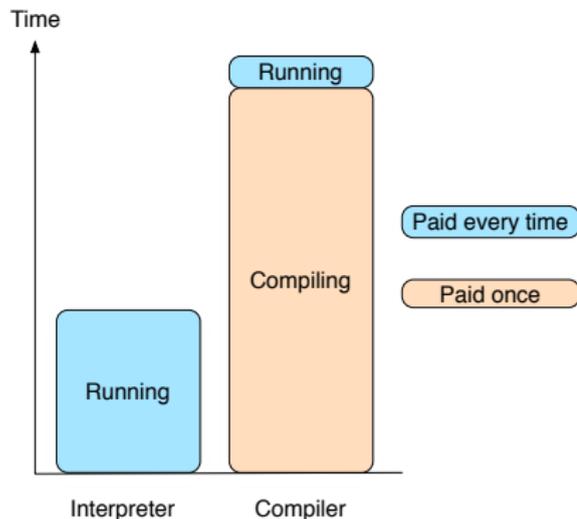
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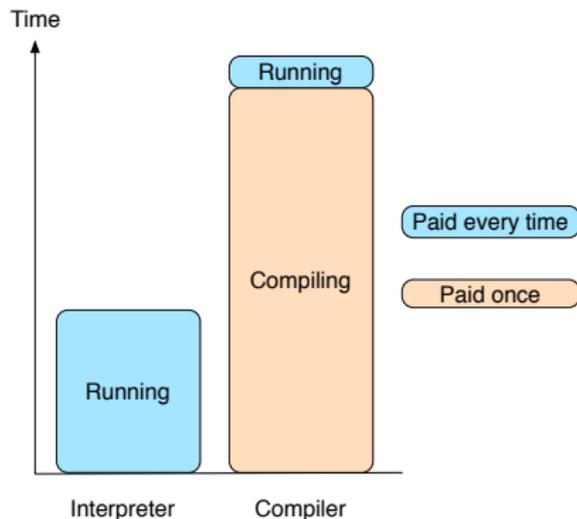
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Combine this with the Pareto principle, and you have a potent weapon at hand.

# Pareto principle, aka 80-20 rule

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Noticed:

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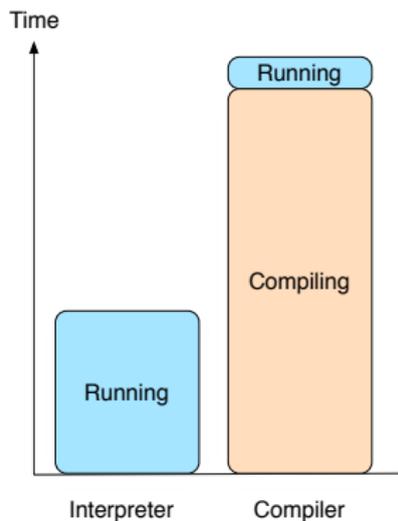
The great majority of a program's execution time is spent running in a tiny fragment of the code.

Such code is referred to as **hot**.

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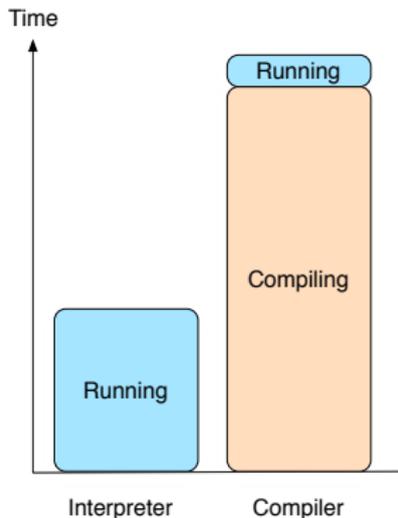
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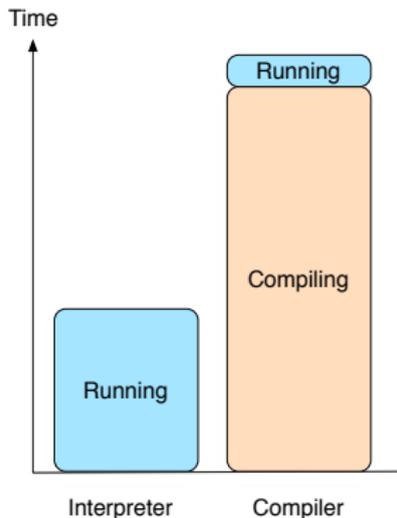
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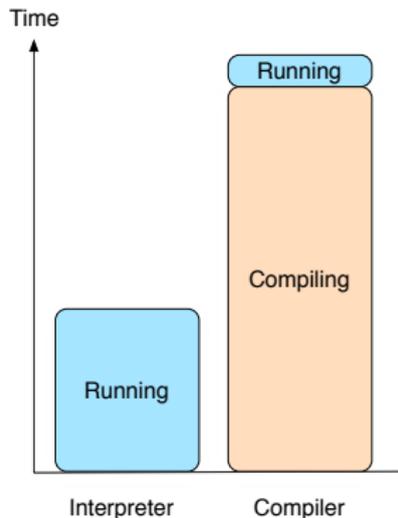


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Pareto's principle tells us that (typically) a program contains some hot code.

With the information available at run-time, we can aggressively optimise such hot code, and get a massive speed-up. The rest is interpreted. Sluggishness of interpretation doesn't matter, because it's only a fraction of program execution time.

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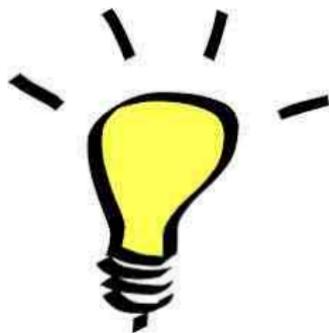


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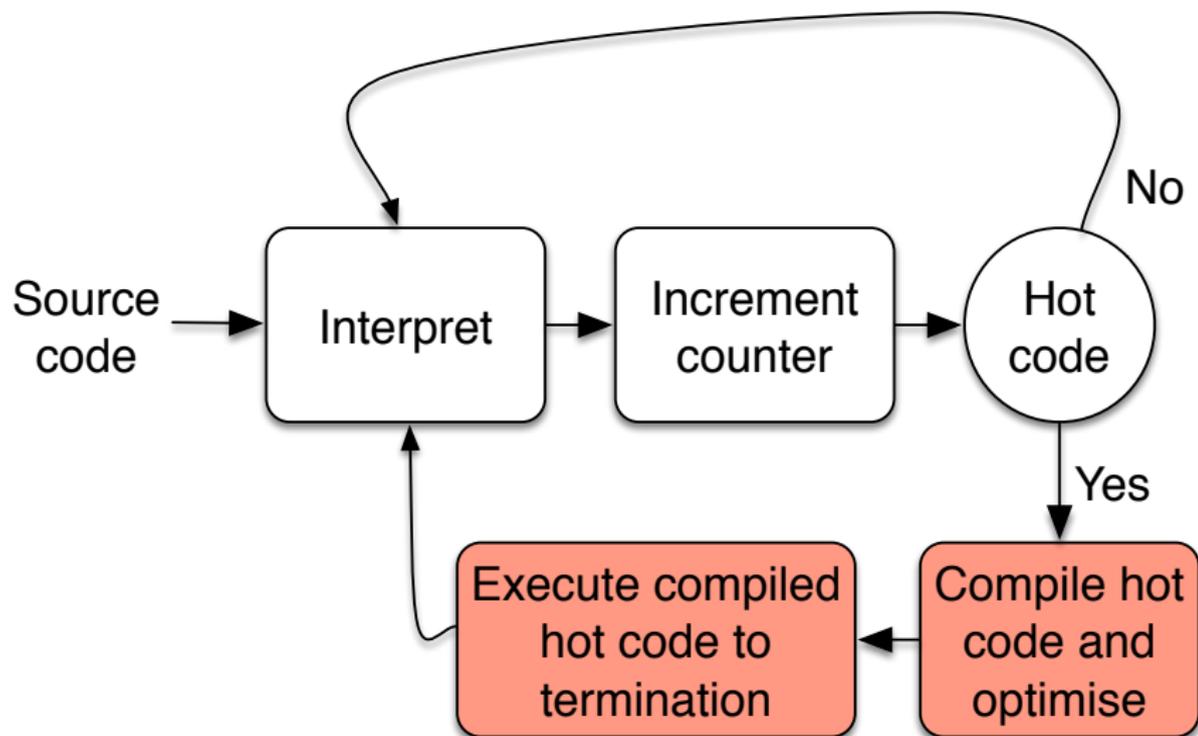
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When the compiled code terminates, we switch back to interpretation.

In a picture

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# Aside

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This is because at the beginning, everything is interpreted, hence slow. Then JIT compilation starts, also slow.

## Aside

Have you noticed that Java programs start up quite slowly?

This is because at the beginning, everything is interpreted, hence slow. Then JIT compilation starts, also slow.

Eventually, the hot code is detected and compiled with a great deal of optimisation. Then execution gets really fast.

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So what's next in compiler technology? Let me introduce you to  
...

# Tracing JIT compilers

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for ( x = 1 to 1000000 )  
  for ( y = 1 to 1000000 )  
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Clearly the `try-catch` block is an innermost loop, so potentially hot code. But if the programmer does a good job, the exception handling will never be triggered. Yet we have all this exception handling code (tends to be large) in the hot loop. This causes all manner of problems, e.g. cache locality is destroyed.

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Why can't we use counters? Yes but ... counters only give us some relevant information ... for good optimisation we need more information. **Traces** give us this information. What are traces?

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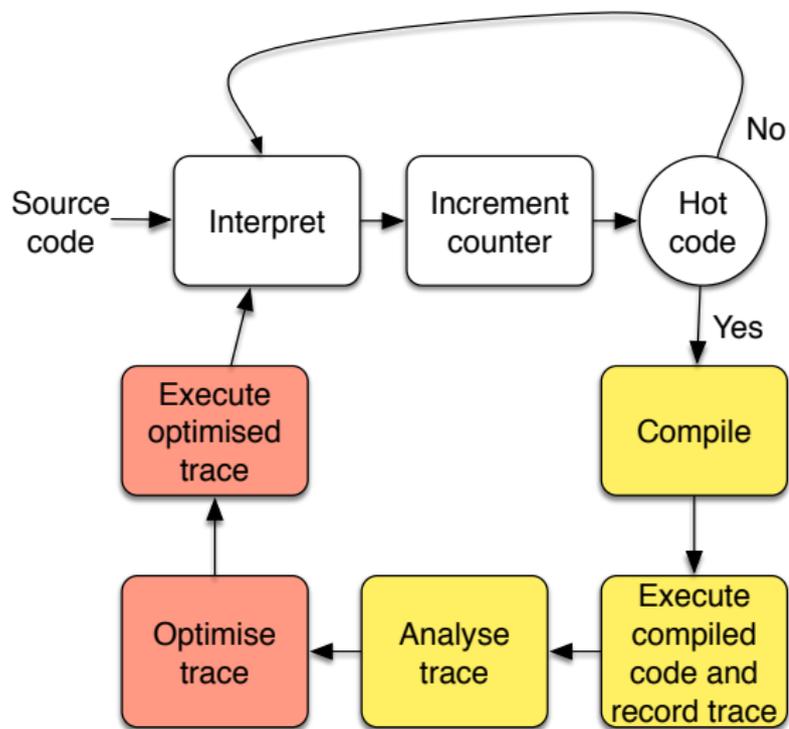
Based on the analysis another compiler generates another (highly optimised) executable, which is then run to termination, then control goes back to interpreter.

# Tracing JIT compilers

Analysing and optimising the trace:

- ▶ Find out if variables change type in the loop, if not, move type-checking out of the loop. (For dynamically typed languages.)
- ▶ Find out if object change type in the loop, if not, use short-cut method invocations, no need to go via method table.
- ▶ Let the interpreter handle the rarely used parts of the hot loop (e.g. error handling).
- ▶ ...
- ▶ Finally, enter the third phase, the 'normal' execution of the optimised trace.

# A tracing JIT compiler in a picture



## Difficulties

As with normal JIT compilers, we have to orchestrate the interplay of all these compiler phases, e.g.: Handover of control from interpreter to compiler, to tracing, to execution of optimised trace, and back. Garbage collection, exceptions, concurrency etc must all also work.

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Hard to say exactly who uses what (e.g. Apple Safari) since companies rarely say what they're using. They can use more than one. Trade secrets.

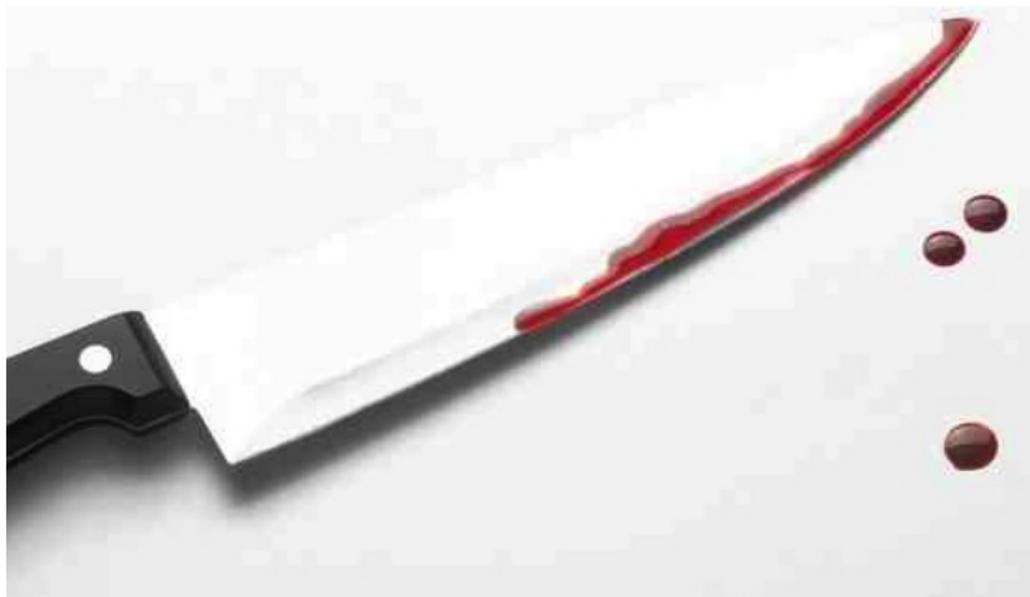
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The problem is that interpreter loops are the kinds of loops that JITers do not optimise well. Let's explain this in detail.

# Why JIT compilers can't optimise interpreter loops

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Now JIT compilers are really good at optimising loops, why do they fail with interpreter loops?

## Key requirements for good JIT optimisation of loops

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Last requirement is violated in interpreter loops.

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This gives rise to something like the following bytecode

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loop:  
    br r17 exit  
    add r21 r33 r21  
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Let's have bytecode and bytecode interpreter side-by-side:

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Now every round of the interpreter takes a different branch. The tracing JIT can just optimise one branch through the loop. This is the worst case scenario: we pay the price of tracing, optimisation (since loop is executed a lot), only to throw away the optimisation and go back to interpretation.

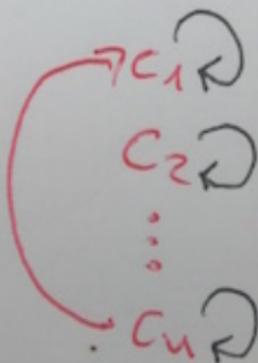
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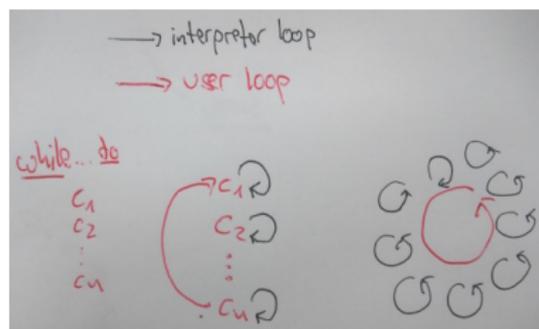
→ user loop

while... do

$C_1$   
 $C_2$   
⋮  
 $C_n$

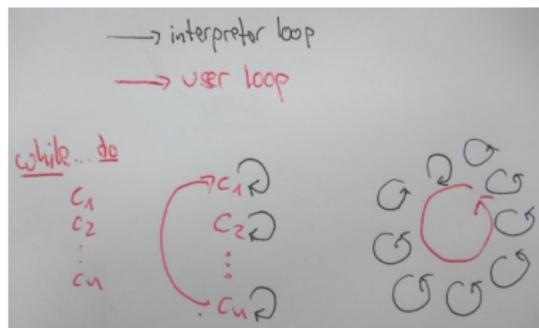


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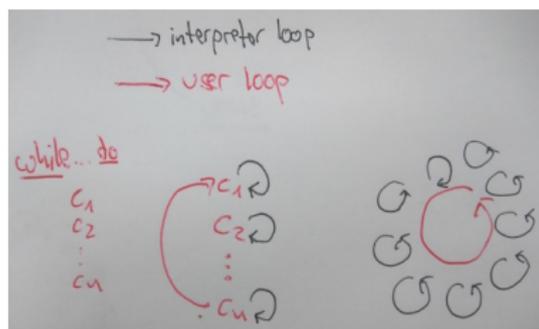
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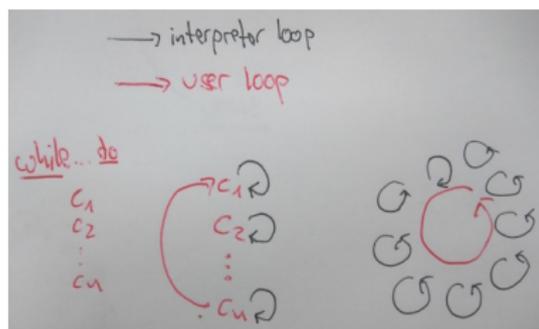


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This is too difficult to detect for profiling, since user programs can vary greatly.

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The interpreter **writer** knows what the user loops are like:

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The idea of meta-tracing is to let the interpreter writer **annotate** the interpreter code with 'hooks' that tell the tracing JIT compiler where user loops start and end. The profiler can then identify the hot loops in (the interpretation of) user code.

## Why can't interpreter loops be JITed?

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while true do:
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It is simple to annotate an interpreter.

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The tracing JIT from (1) can be reused for an unlimited number of language interpreters. Once a meta-tracing JIT is available, we can easily develop new languages and have high-performance compilers for them (almost) for free.

## Meta-tracing as game changer in PL development

The real advantage of this is that it divides the problem of developing high-performance JIT compilers for a language into several parts, each of which separately is much more manageable:

1. Develop a (meta-)tracing JIT compiler. **Hard**, but needs to be **done only once**.
2. Develop an interpreter for the given source language. **Easy!**
3. Add annotations in the interpreter to expose user loops. **Easy!**
4. Run the interpreter using the tracing JIT from (1). **Easy!**

The tracing JIT from (1) can be reused for an unlimited number of language interpreters. Once a meta-tracing JIT is available, we can easily develop new languages and have high-performance compilers for them (almost) for free.

The PyPy meta-tracing framework runs Python substantially faster than e.g. the CPython framework.

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JIT compilers work best for languages that do a lot of stuff at run-time (e.g. type-checking).

For bare-bones languages like C, there is little to optimise at run-time, and code generated by a conventional C compiler with heavy (hence slow) optimisation will almost always beat a modern JIT compiler.

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Much work left to be done.

Interested?

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Feel free to talk to me about this.



Happy  
New year

The text 'Happy New year' is rendered in a highly stylized, multi-colored font. Each letter is filled with a different color: 'H' is red, 'a' is green, 'p' is blue, 'p' is red, 'y' is black, 'N' is red, 'e' is blue, 'w' is black, 'y' is purple, 'e' is orange, and 'a' is green. The letters have a distressed, ink-splattered texture. Long, thin, curved lines extend from the bottom of the letters 'y' and 'a' in the second row, and from the 'y' in the first row.